

## ASTRONOMY 1100. INTRODUCTION TO ASTROPHYSICS

### Assignment 3.

Due Date: March 19, 2014.

1. A solar flare is observed near the centre of the Sun's disk in white light imaging, and from spectroscopic observations it is determined that the ionized material in the ejecta is heading toward the Earth at a speed of  $800 \text{ km s}^{-1}$ . Calculate how long it will take for the flare ejecta to reach the Earth, *i.e.* how long it will be before the effects of the flare are evident in fluctuations of the Earth's geomagnetic field.
2. If the current rate of hydrogen burning in the Sun remains constant, what fraction of the Sun's mass will be converted into helium over the next  $5 \times 10^9$  years? By how much will the total mass of the Sun have been reduced over the same time interval?
3. The star Aldebaran ( $\alpha$  Tauri) is a K5 III giant. According to measurements obtained from the *HIPPARCOS* mission, Aldebaran has a trigonometric parallax of  $\pi = 0''.05009 \pm 0''.00158$ . Determine the distance to Aldebaran in parsecs. Also determine the uncertainty in that value (in parsecs).
4. Aldebaran (Question 3) has an observed photoelectric visual magnitude of  $V = +0.87$ . Determine the star's absolute visual magnitude,  $M_V$ . Is the value typical of a K giant? [Hint: See Figure 19–13 of the textbook.]
5. The *HIPPARCOS* Mission also provided data on the proper motion of Aldebaran (Question 3), and lists its proper motion as  $+0.06278$  arcsecond per year in right ascension and  $-0.18936$  arcsecond per year in declination. Determine the net proper motion of Aldebaran, and use the resulting value with the answer to Question 3 to establish the tangential velocity of the star. Aldebaran also has a radial velocity of  $+54 \text{ km s}^{-1}$ . What is the star's total space velocity with respect to the Sun?
6. As viewed from Earth, the Sun has a visual magnitude of  $V = -26.75$ . What will the Sun's brightness be, in magnitude units, as seen from the surface of one of Saturn's satellites? Saturn's mean distance from the Sun is 9.54 A.U.
7. At one stage during its birth, the protosun had a luminosity of  $1000 L_{\odot}$  and a surface temperature of about 1000 K. What was its radius at that time? Express your answer in terms of the present-day solar radius, in kilometres, and in astronomical units (A.U.).
8. During the helium-burning stage of stellar evolution, three helium nuclei  ${}^4\text{He}$ , each of mass 4.002603 atomic mass units, are converted into a single carbon nucleus  ${}^{12}\text{C}$ , of mass 12.000000 atomic mass units, *i.e.*  $3 {}^4\text{He} \rightarrow {}^{12}\text{C}$ , where one atomic mass unit equals  $1.66054 \times 10^{-27} \text{ kg}$ . Calculate the amount of energy released in one such set of reactions. During the helium burning stages for high-mass stars, a star's luminosity is typically on the order of  $1500 L_{\odot}$  or more. How long would it take for a typical star of this type to use up  $1 M_{\odot}$  of helium fuel?