

**Study of the Spin Structure
Functions
of the Neutron at Low Q^2
with Polarized ^3He**

presented by

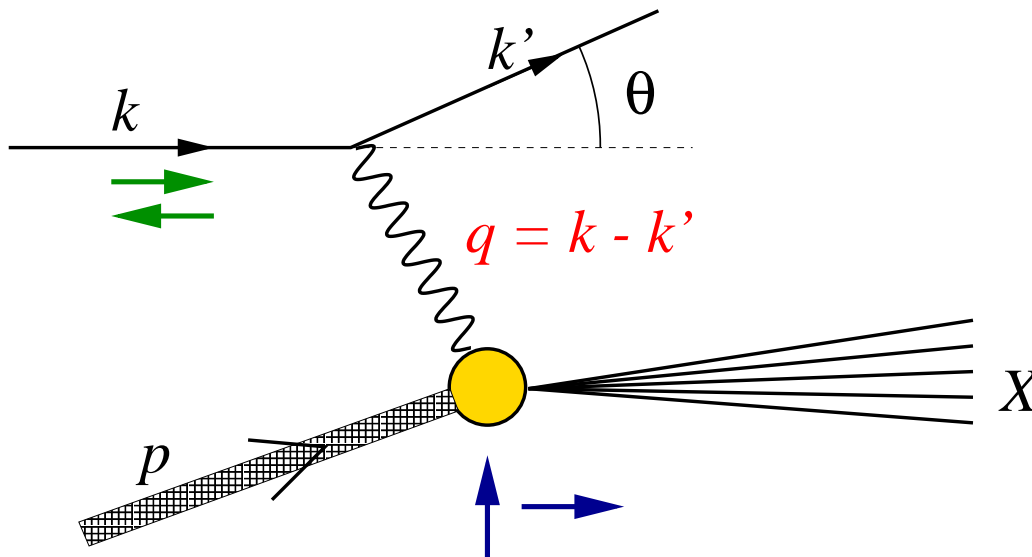
Seonho Choi

Temple University

For JLab E94010 Collaboration

LowQ 03
July 17, 2003

Inclusive Electron Scattering



- Four-momentum transfer

$$Q^2 = -q^2 = 4EE' \sin^2 \frac{\theta}{2}$$

- Energy transfer to the hadron

$$\nu = E - E'$$

- Mass of the hadronic residual (or invariant mass)

$$W = \sqrt{(p + q)^2} = \sqrt{M_N^2 + 2M_N\nu - Q^2}$$

- Bjorken scaling variable

$$x = \frac{Q^2}{2M_N\nu}$$

Structure Functions

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{4\alpha^2 E'^2 \cos^2 \frac{\theta}{2}}{Q^4} \left[\frac{F_2}{\nu} + 2 \frac{F_1}{M} \tan^2 \frac{\theta}{2} \right]$$

$$\frac{d^2\sigma}{dE' d\Omega} (\downarrow\uparrow - \uparrow\uparrow) = \frac{4\alpha^2 E'}{MQ^2 \nu E} \left[(E + E' \cos \theta) g_1 - \frac{Q^2}{\nu} g_2 \right]$$

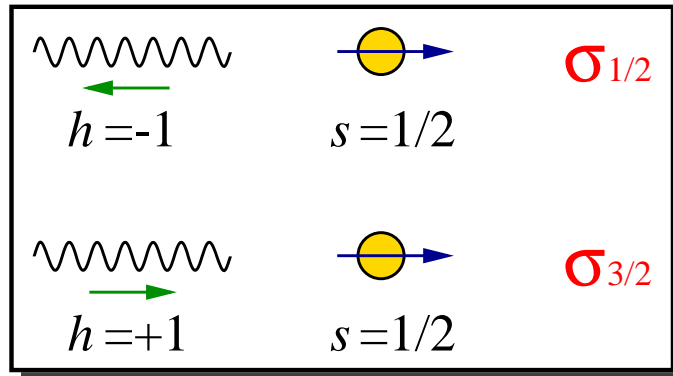
$$\frac{d^2\sigma}{dE' d\Omega} (\downarrow\Rightarrow - \uparrow\Rightarrow) = \frac{4\alpha^2 \sin \theta E'^2}{MQ^2 E \nu^2} (\nu g_1 + 2E g_2)$$

$$\left. \begin{aligned} F_1(x) &= \frac{1}{2} \sum_i e_i^2 [q_i(x) + \bar{q}_i(x)] \\ F_2(x) &= \sum_i e_i^2 x [q_i(x) + \bar{q}_i(x)] \end{aligned} \right\} F_2(x) = 2x F_1(x) \text{ (Callan-Gross)}$$

$$g_1(x) = \frac{1}{2} \sum_i e_i^2 \Delta q_i(x)$$

$$\Delta q_i(x) = q_i^+(x) + \bar{q}_i^+(x) - q_i^-(x) - \bar{q}_i^-(x)$$

Gerasimov-Drell-Hearn Sum Rule



$$I_{\text{GDH}} = \int_{\nu_{\text{th}}}^{\infty} (\sigma_{1/2} - \sigma_{3/2}) \frac{d\nu}{\nu} = -\frac{2\pi^2 \alpha}{M^2} \kappa^2$$

κ : the nucleon anomalous magnetic moment

$$I_{\text{GDH}}^{\text{proton}} = -204.8 \mu\text{b} \quad I_{\text{GDH}}^{\text{neutron}} = -233.2 \mu\text{b}$$

- Derived from very general principles applied to the forward Compton amplitude on the nucleon
- Valid for real photon ($Q^2 = 0$) absorption

GDH Integral at $Q^2 > 0$

$$\begin{aligned} I_{\text{GDH}} &\equiv \int (1-x)(\sigma_{1/2} - \sigma_{3/2}) \frac{d\nu}{\nu} \\ &= \int \frac{8\pi^2\alpha}{M\nu} \left(g_1 - \frac{Q^2}{\nu^2} g_2 \right) \frac{d\nu}{\nu} \end{aligned}$$

Chiral perturbation theory calculation at small Q^2 gives*

$$\begin{aligned} S_1(0, Q^2) &= 4 \int G_1(\nu, Q^2) \frac{d\nu}{\nu} \\ &= \int \frac{4}{M\nu} g_1 \frac{d\nu}{\nu} \\ \lim_{\nu \rightarrow 0} \frac{S_2(\nu, Q^2)}{\nu} &= 4 \int G_2(\nu, Q^2) \frac{d\nu}{\nu^2} \\ &= \int \frac{4}{M\nu} \frac{g_2}{\nu^2} \frac{d\nu}{\nu} \end{aligned}$$

As a result,

$$I_{\text{GDH}} = 2\pi^2\alpha \left[S_1(0, Q^2) - Q^2 \left. \frac{S_2(\nu, Q^2)}{\nu} \right|_{\nu \rightarrow 0} \right]$$

* Xiangdong Ji and Jonathan Osborne, J. Phys. **G27** 127 (2001).

Integrals of Structure Functions

$$\Gamma_1(Q^2) = \int_0^1 g_1(x, Q^2) dx$$

Bjorken Sum Rule

$$\Gamma_1^p(Q^2) - \Gamma_1^n(Q^2) = \frac{g_A}{6} \quad \text{as } Q^2 \rightarrow \infty$$

$$\Gamma_2(Q^2) = \int_0^1 g_2(x, Q^2) dx$$

Burkhardt-Cottingham Sum Rule

$$\Gamma_2(Q^2) = 0 \quad \text{at every } Q^2$$

$$\begin{aligned} d_2 &= 3 \int_0^1 x^2 (g_2(x, Q^2) - g_2^{WW}(x, Q^2)) dx \\ &= \int_0^1 x^2 (2g_1(x, Q^2) + 3g_2(x, Q^2)) dx \end{aligned}$$

$$g_2^{WW}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 \frac{g_1(y)}{y} dy$$

$d_2(Q^2)$ measures twist 3 and higher contributions to g_2

Cont.

Spin Polarizabilities

$$\gamma_0(Q^2) = \frac{16M^2\alpha_{\text{em}}}{Q^6} \int_0^{x_0} dx x^2 \left\{ g_1(x, Q^2) - \frac{4M^2}{Q^2} g_2(x, Q^2) \right\}$$

$$\delta_{LT}(Q^2) = \frac{16M^2\alpha_{\text{em}}}{Q^6} \int_0^{x_0} dx x^2 \{ g_1(x, Q^2) + g_2(x, Q^2) \}$$

$$\delta_{LT}(Q^2) \rightarrow \frac{1}{3} \gamma_0(Q^2), \quad Q^2 \rightarrow \infty$$

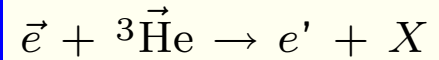
$I_3(Q^2)$

$$I_3(Q^2) = \frac{2M^2}{Q^2} \int_0^{x_0} dx \{ g_1(x, Q^2) + g_2(x, Q^2) \}$$

$$I_3(0) = \frac{e\kappa}{4} \quad \text{if BC sum rule holds}$$

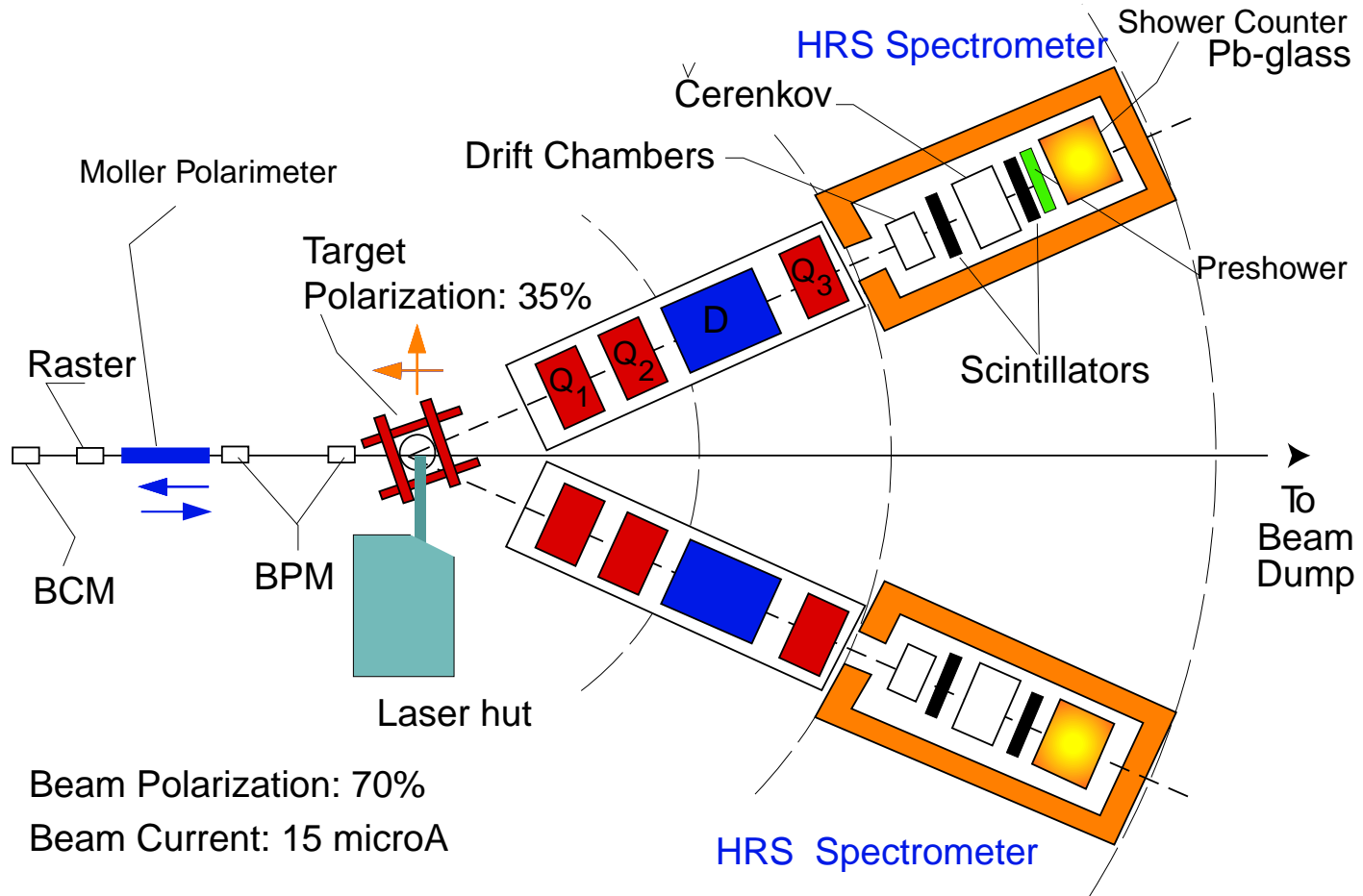
Spin Duality

Summary of the Experiment

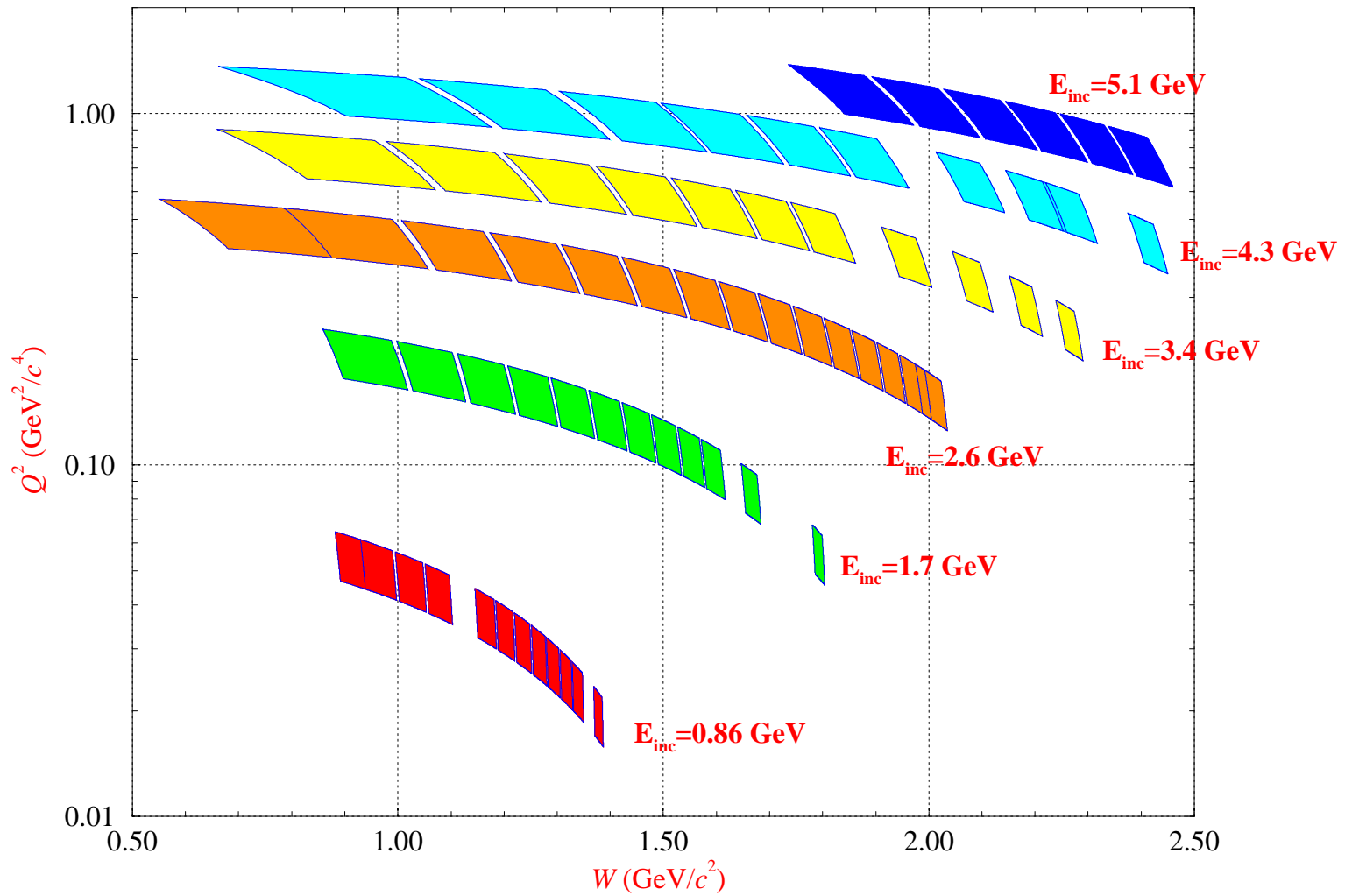


- **Beam** : Polarized electron beam at Jefferson Lab.
 - Energy : 6 beam energies from 0.86 GeV to 5.1 GeV
 - Current : 5 to 15 μA
 - Polarization : $> 70\%$ (GaAs crystal)
- **Target** : Polarized ${}^3\text{He}$ target (Optical pumping)
 - Polarization : average 35%
 - Density : ~ 10 atm
 - Length : 40 cm with window thickness of 0.1 mm
- **Scattering angle** : 15.5°
- **Detectors** : JLab Hall-A Spectrometers

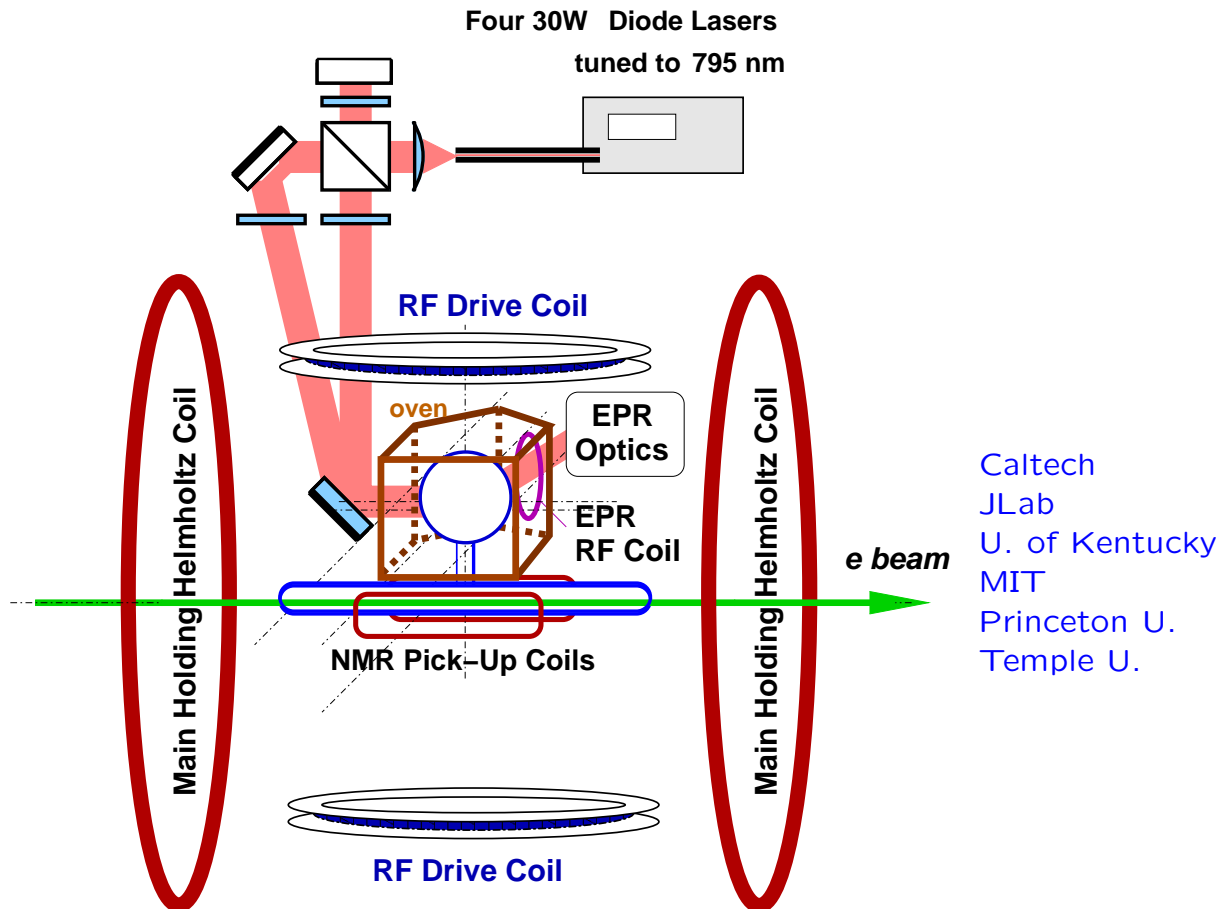
JLab E94010 Floor Configuration



JLab E94010 Kinematic Coverage

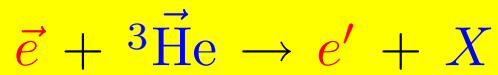


Polarized ^3He Target Setup



- NMR and EPR techniques for polarization monitoring.
- Elastic asymmetry measurement for current induced depolarization.
- Target used successfully for several polarized ^3He experiments.
- Target length 40 cm, window thickness 0.1 mm.

Analysis Schematics



$$\sigma_{\downarrow\uparrow}$$

$$\sigma_{\uparrow\uparrow}$$

$$\sigma_{\downarrow\Rightarrow}$$

$$\sigma_{\uparrow\Rightarrow}$$

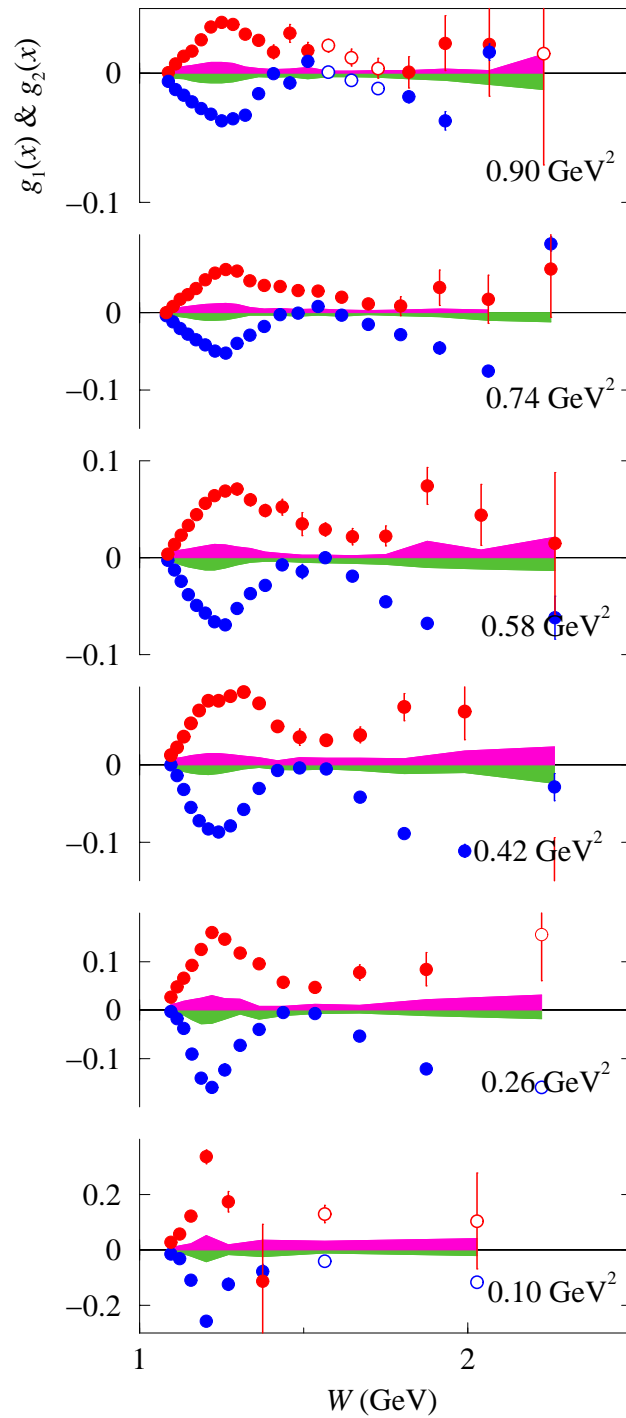
$$\Delta\sigma_{\parallel} = \frac{1}{P_b P_t} (\sigma_{\downarrow\uparrow} - \sigma_{\uparrow\uparrow})$$

$$\Delta\sigma_{\perp} = \frac{1}{P_b P_t} (\sigma_{\downarrow\Rightarrow} - \sigma_{\uparrow\Rightarrow})$$

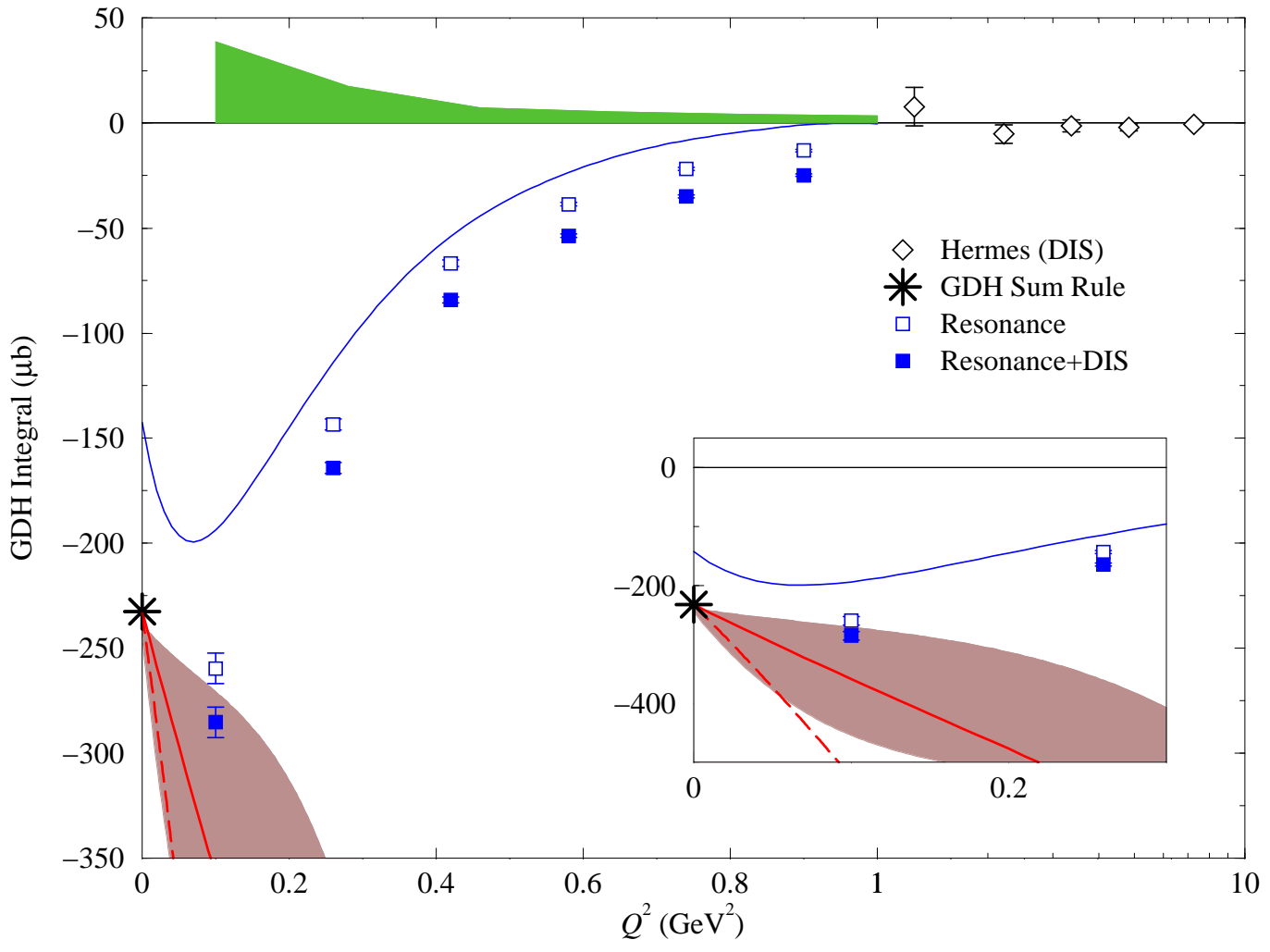
$$g_1, g_2, \sigma_{1/2} - \sigma_{3/2}$$

$$I_{\text{GDH}} = \int_{\nu_{\text{th}}}^{\infty} (1-x)(\sigma_{1/2} - \sigma_{3/2}) \frac{d\nu}{\nu}$$
$$\Gamma_1 = \int_0^1 g_1(x, Q^2) dx$$
$$\Gamma_2 = \int_0^1 g_2(x, Q^2) dx$$

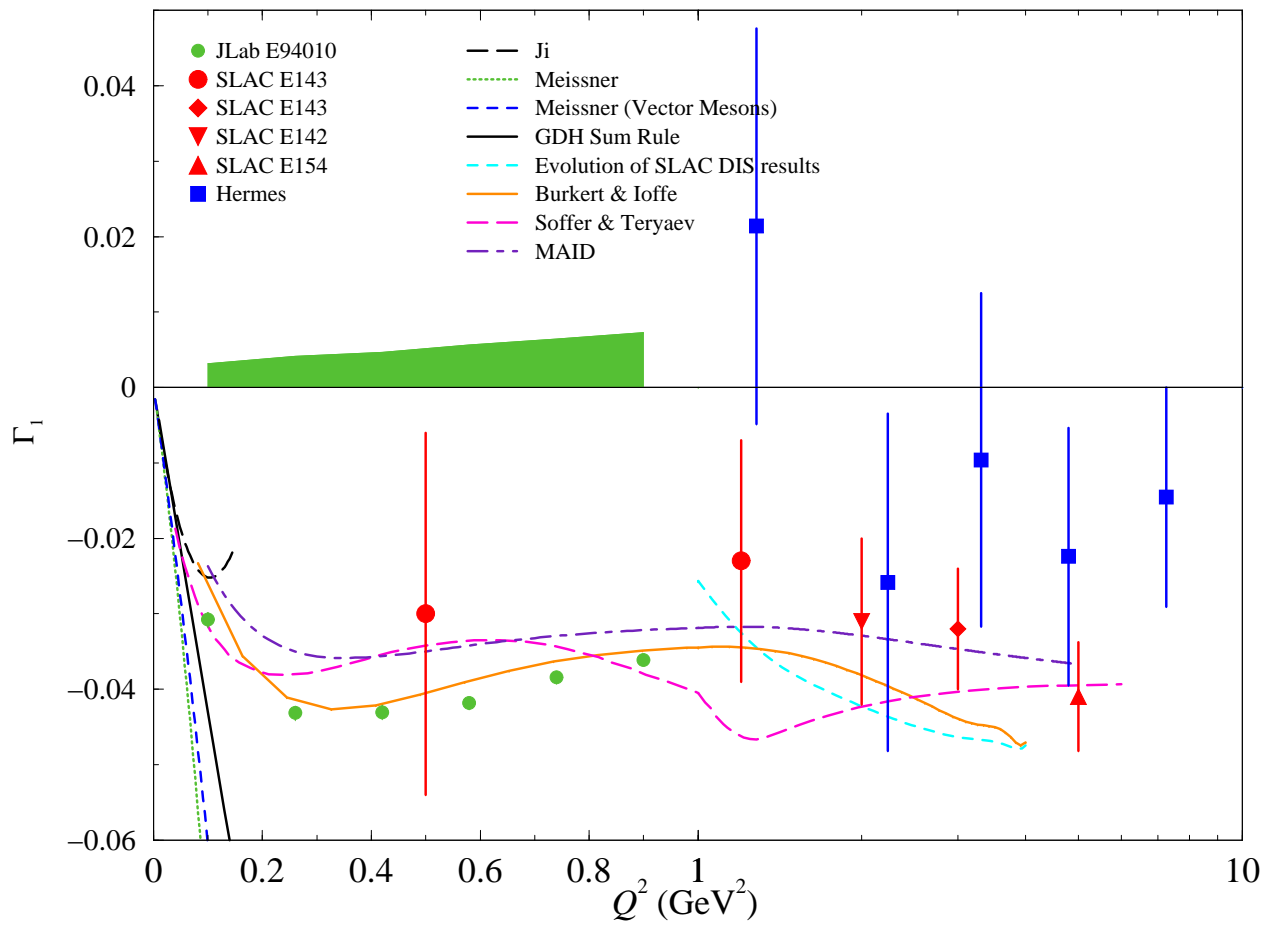
$g_1(x)$ and $g_2(x)$ at Constant Q^2



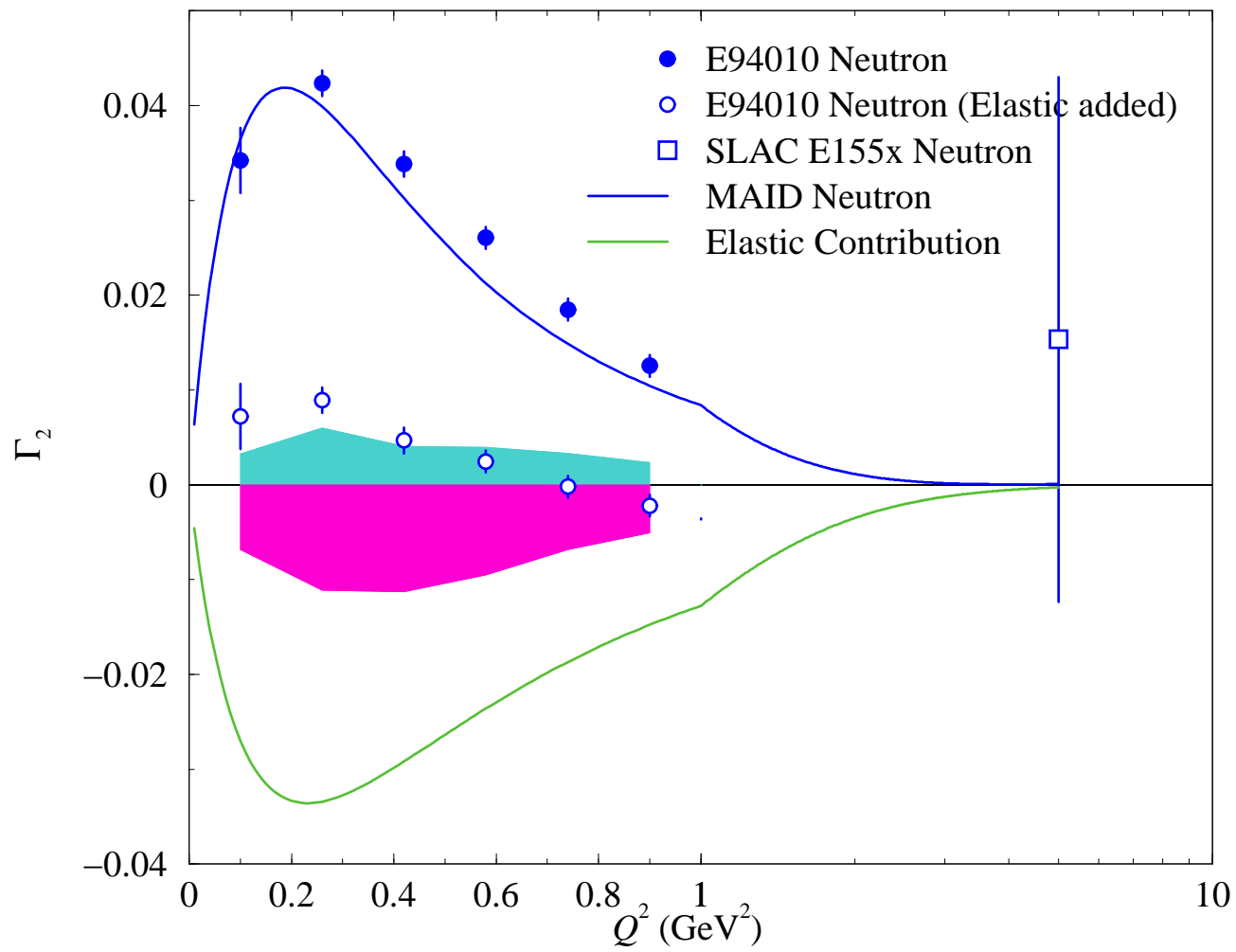
GDH Integral



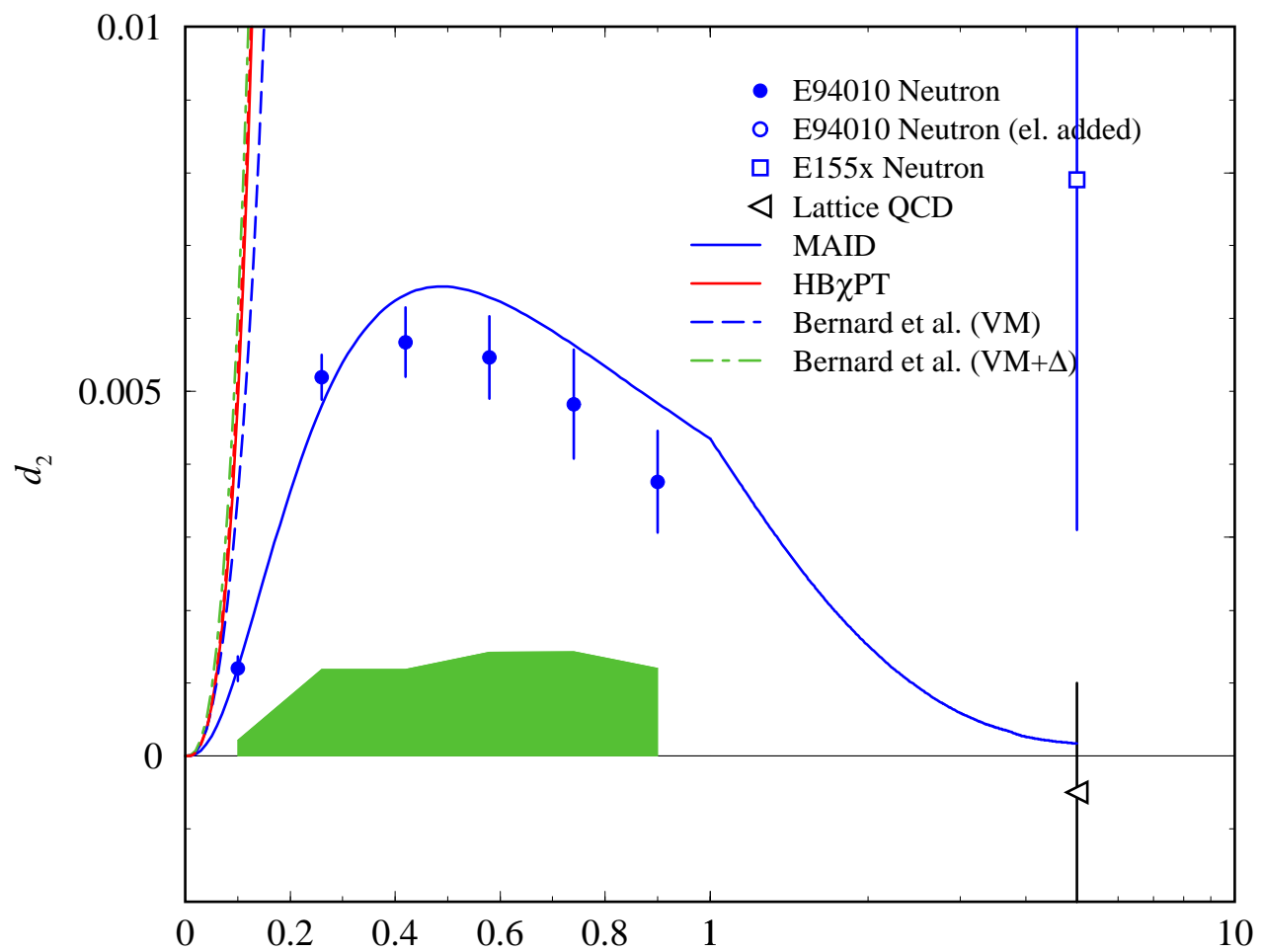
Integral of $g_1(x, Q^2)$



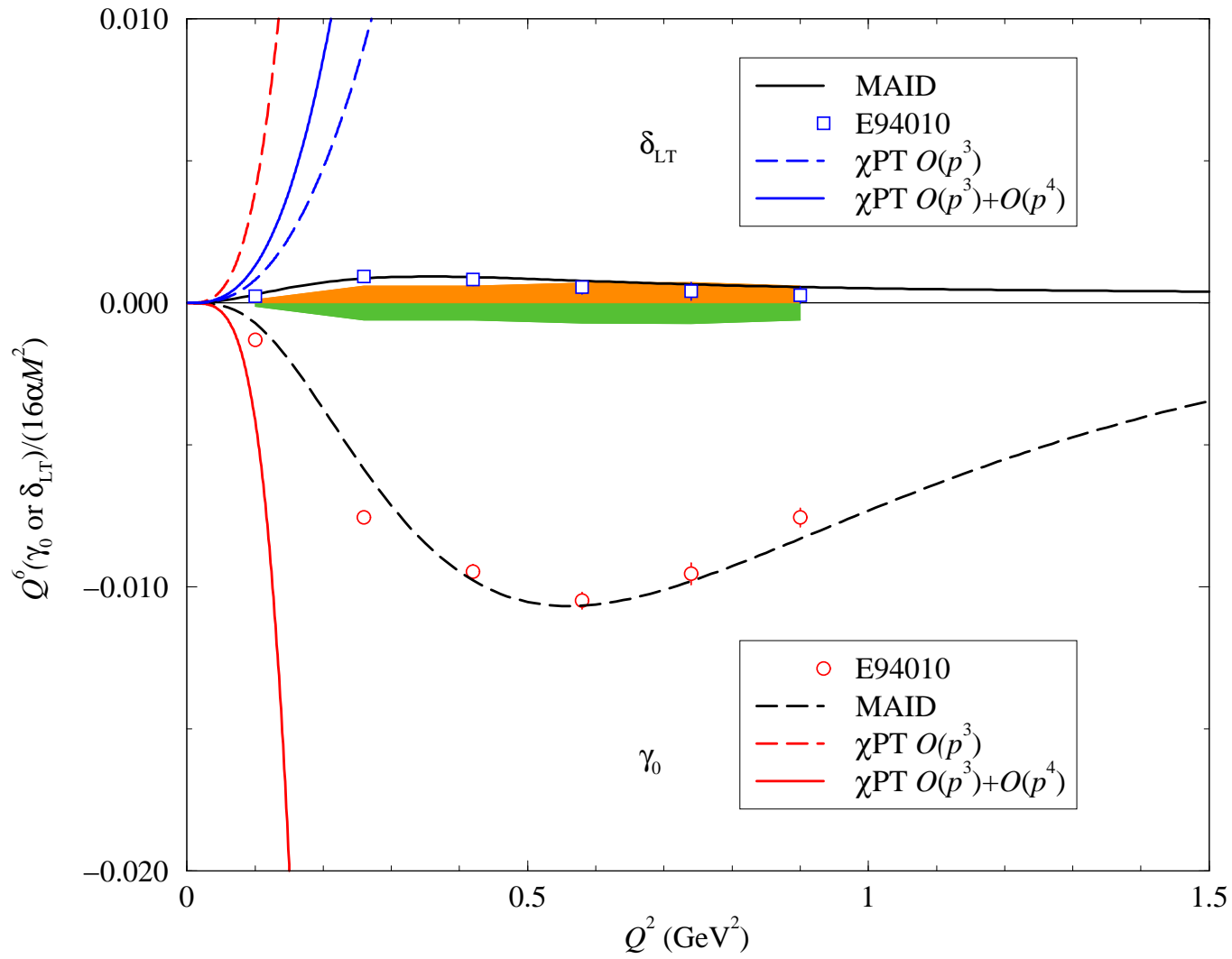
Integral of $g_2(x, Q^2)$



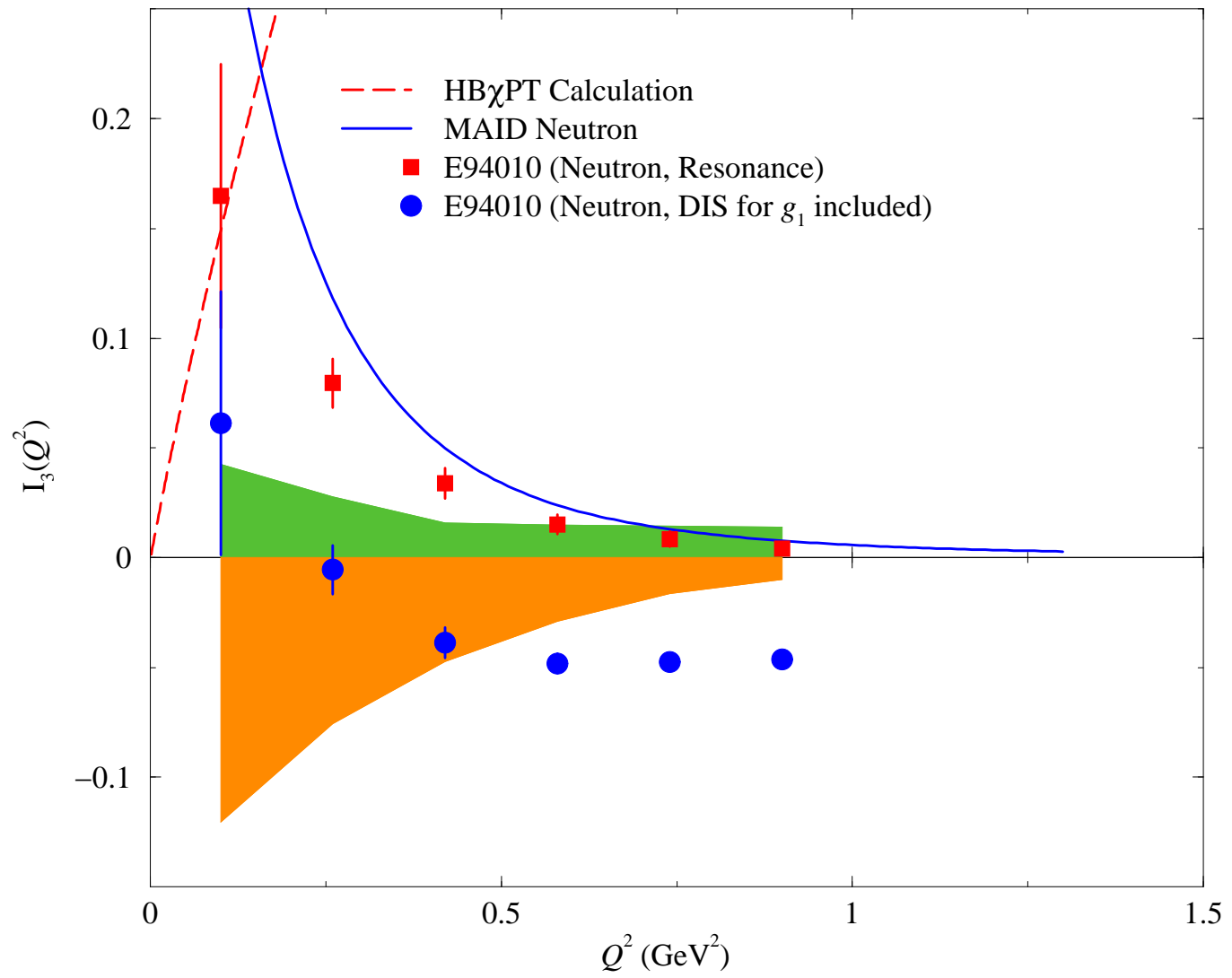
$$d_2(Q^2)$$



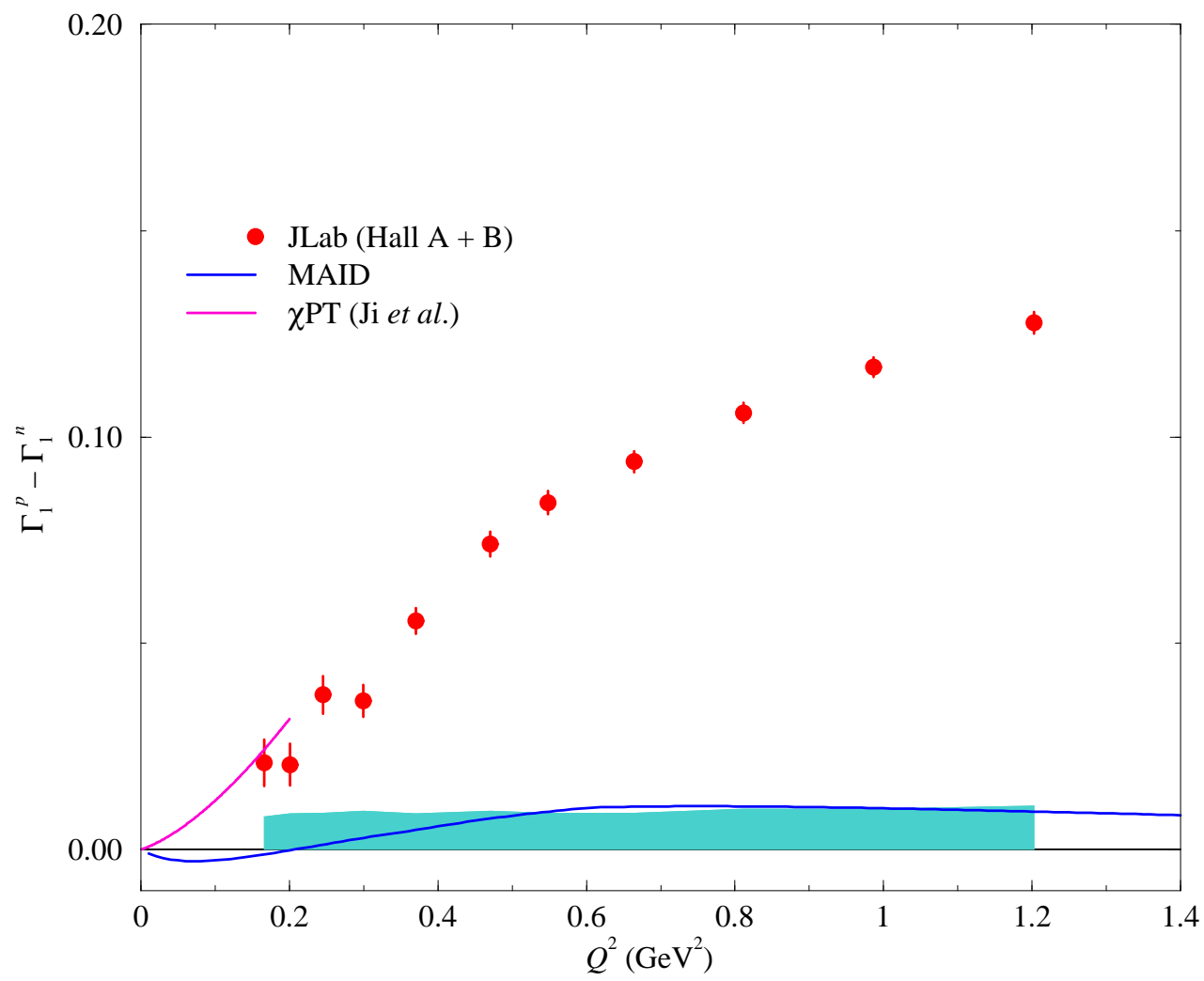
Spin Polarizabilities



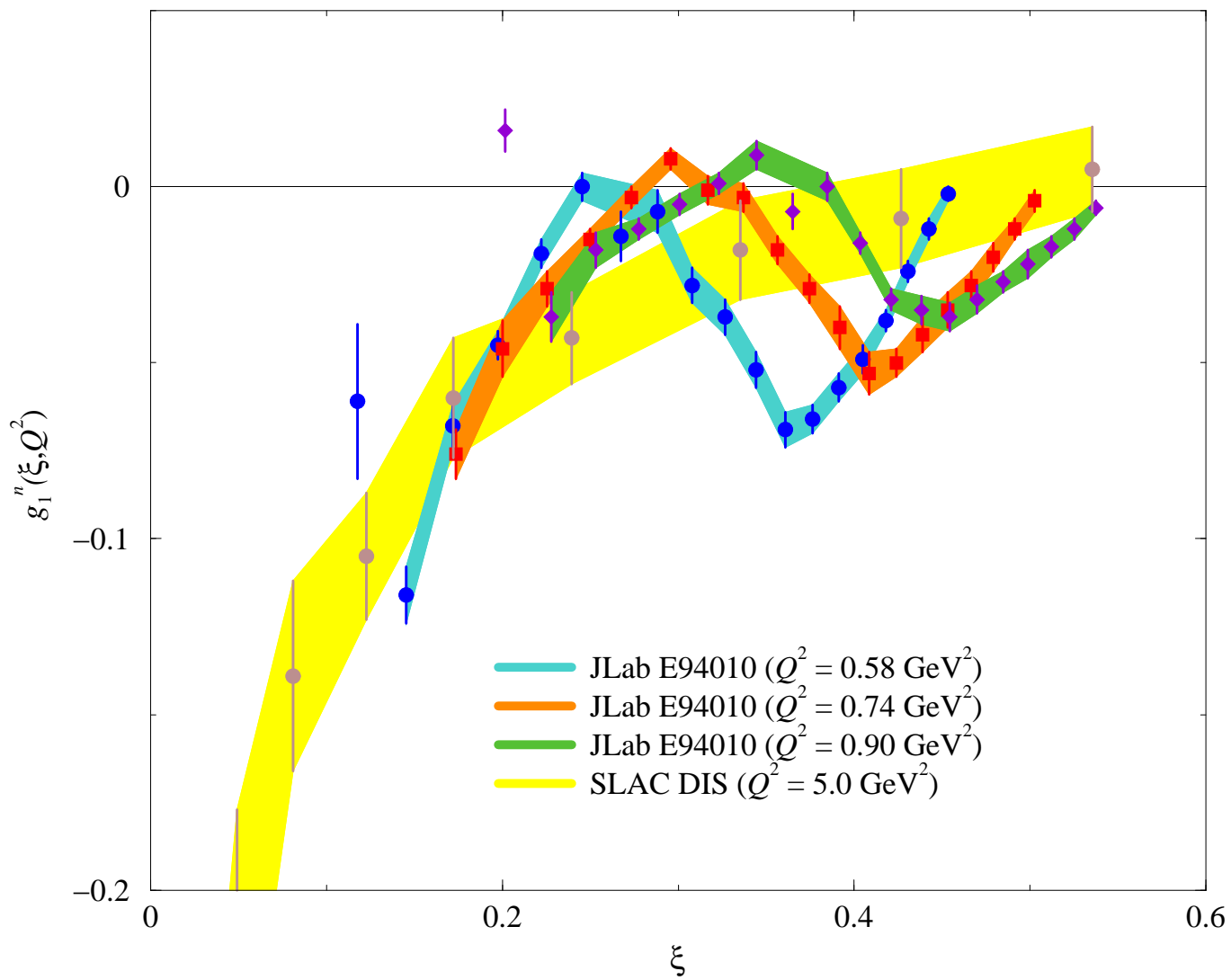
$I_3(Q^2)$



Bjorken Sum



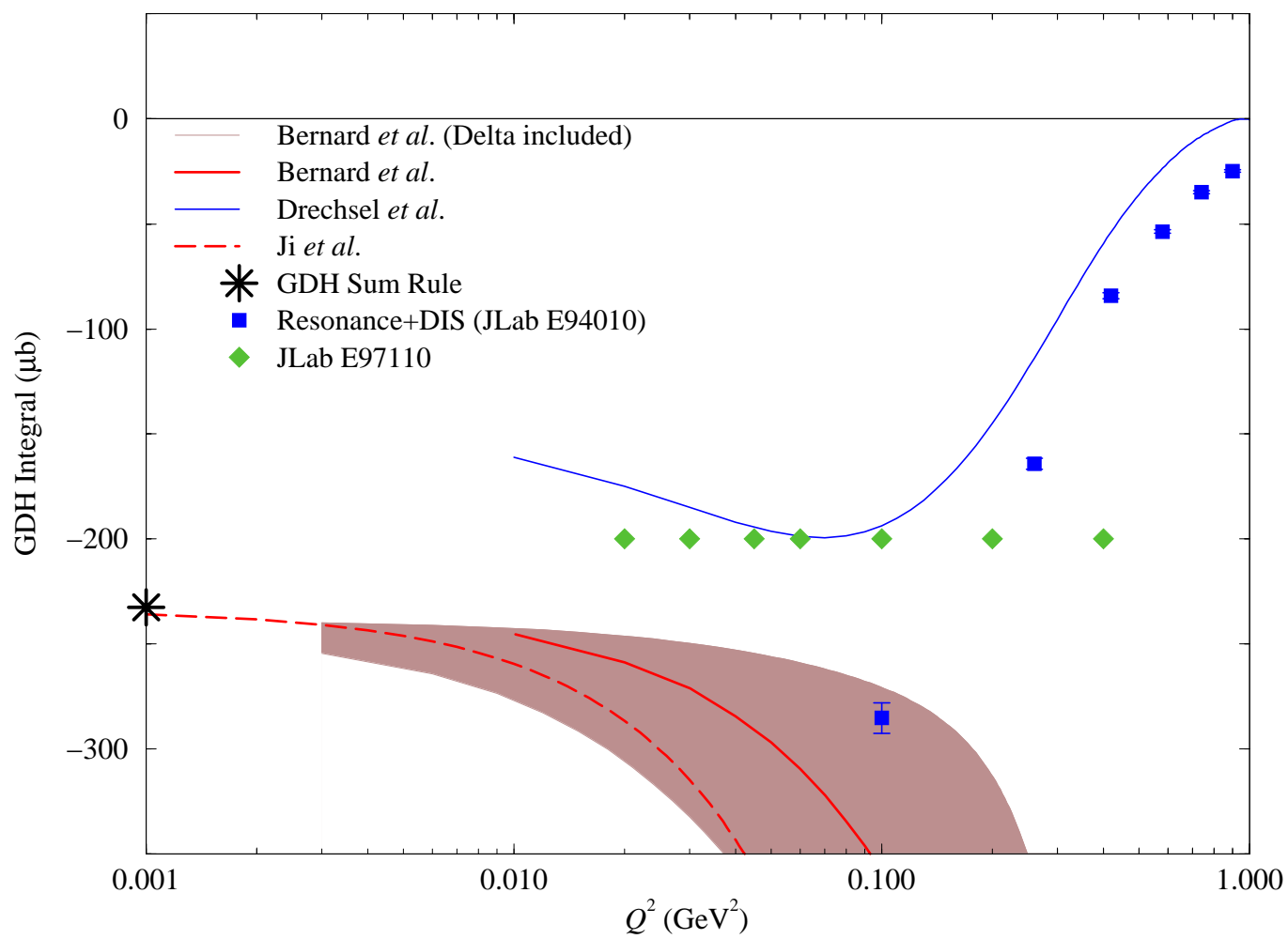
Spin Duality



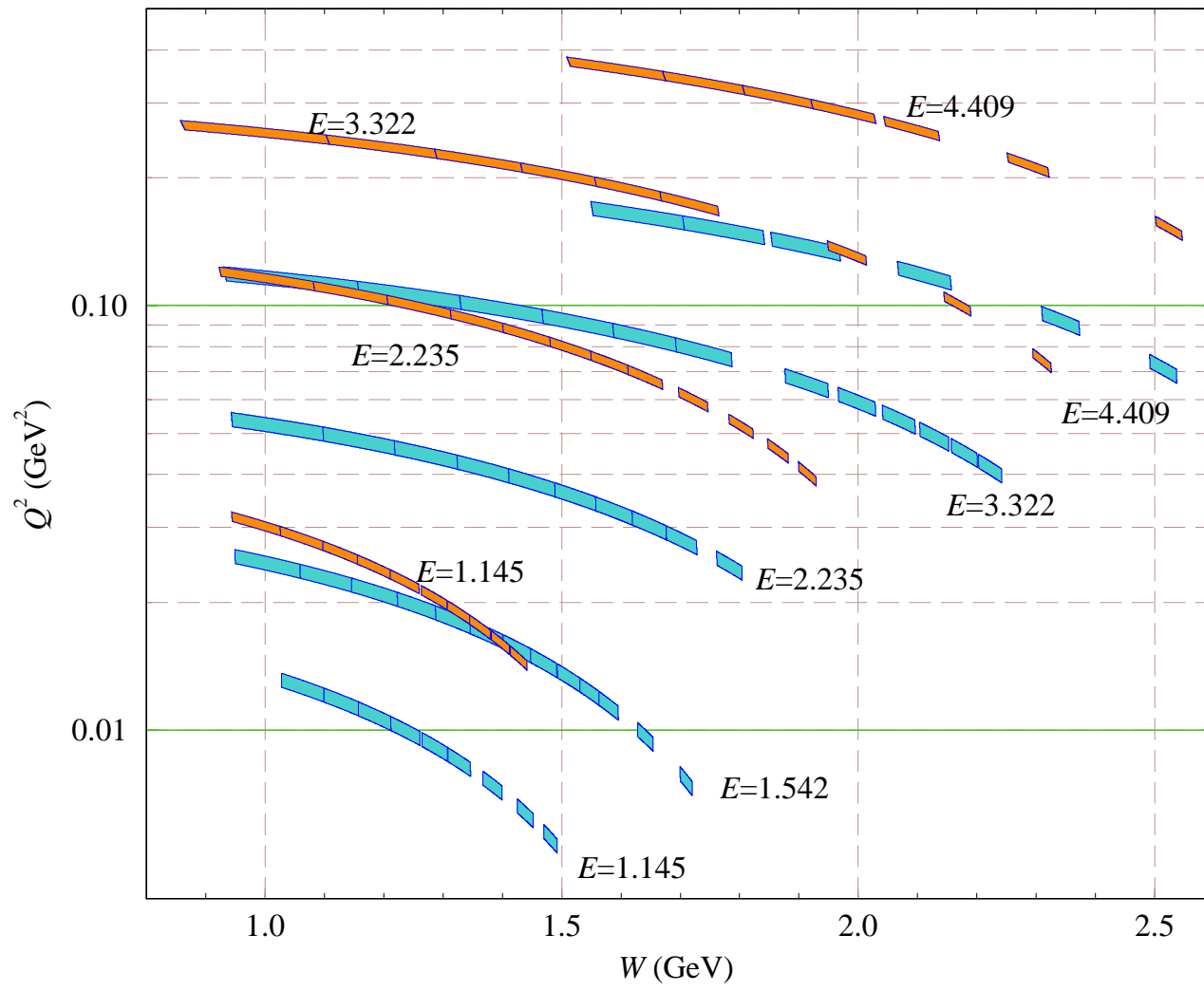
Conclusion

- $g_1(x, Q^2)$ and $g_2(x, Q^2)$ for the **neutron** have been measured at $Q^2 < 1\text{GeV}^2$ region
- Various integrals have been evaluated
 - **GDH Sum Rule**
 - Transition from $Q^2 > 1$ to small Q^2 observed
 - More interesting results expected from future JLab experiment at even smaller Q^2
 - $\Gamma_1(Q^2)$
 - Much improved precision compared to SLAC data
 - With JLab Hall-B data combined, study of Bjorken Sum
 - $\Gamma_2(Q^2)$. $d_2(Q^2)$, $\gamma_0(Q^2)$ and δ_{LT} have been measured at small Q^2 for the first time.
 - Hint of neutron **spin duality** for $g_1(x, Q^2)$ at $Q^2 < 1.0 \text{ GeV}^2$
- Future
 - Small angle GDH experiment
 - Spin duality for the neutron at $1 < Q^2 < 4 \text{ GeV}^2$

JLab E97-110



JLab E97-110 (Kinematics)



Experiment E01-012

Measurement of Neutron (^3He) Spin Structure Functions in the Resonance Region

Spokespeople: N. Liyanage, J.P.Chen, S.Choi

- A precision measurement of neutron spin structure functions in the resonance region up to $Q^2 = 5.5 \text{ GeV}^2$.

Test quark-hadron duality in spin structure functions.

A first test of spin-flavor dependence of duality

- Duality \rightarrow Powerful tool to study very high x behavior.
- **Understanding quark-hadron duality will help us understand confinement of quarks in protons and neutrons**

