

# OPACITY & OPTICAL DEPTH:

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## - INTERACTION OF GAS AND RADIATION

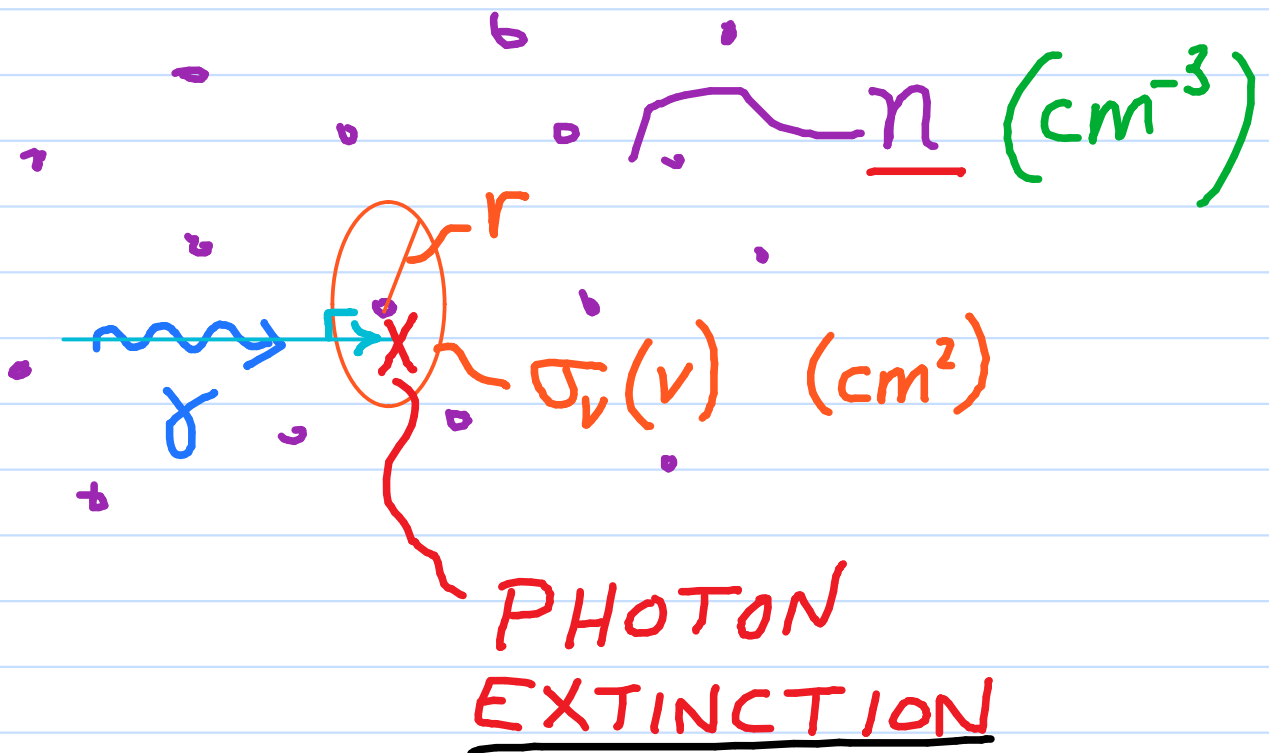
### MONOCHROMATIC INTERACTION

### CROSS-SECTION FOR PHOTONS ( $\gamma$ )

AND GAS PARTICLES,

$$\underline{\sigma_{\gamma}(\nu)} \quad (\text{cm}^2)$$

-  $\nu$  = FREQUENCY (Hz)



# MONOCHROMATIC VOLUME

EXTINCTION COEFFICIENT,

$$\underline{\alpha_\nu(\nu)} \quad (\text{cm}^{-1})$$

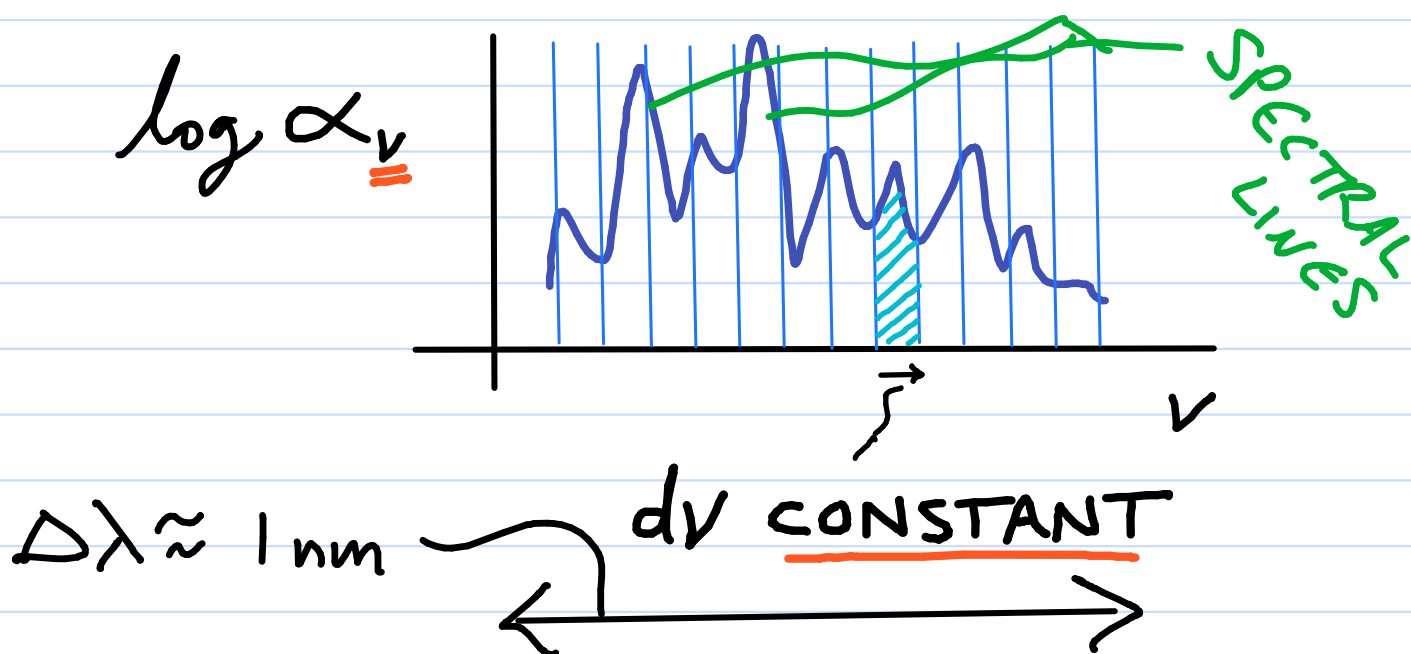
FOR A GAS THAT EXTINGHISHES ONLY:

$$\alpha_\nu(\nu) = n \sigma_\nu(\nu)$$

$\text{cm}^{-3}$                        $\text{cm}^2$

("LINEAR EXTINCTION")

$\alpha_\nu(\nu)$ : A CONTINUOUS  $\nu$  DISTRIBUTION:



# MONOCHROMATIC MASS

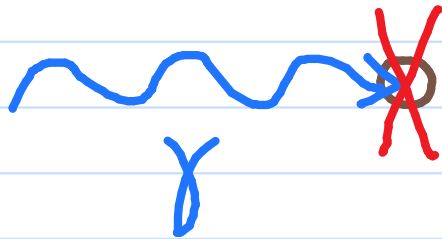
EXTINCTION COEFFICIENT,

$$\underline{\kappa_\nu(\nu)} \quad (\text{cm}^2/\text{g})$$

$$\kappa_\nu(\nu) = \frac{\alpha_\nu(\nu)}{\rho} = \frac{n\sigma_\nu(\nu)}{\rho}$$

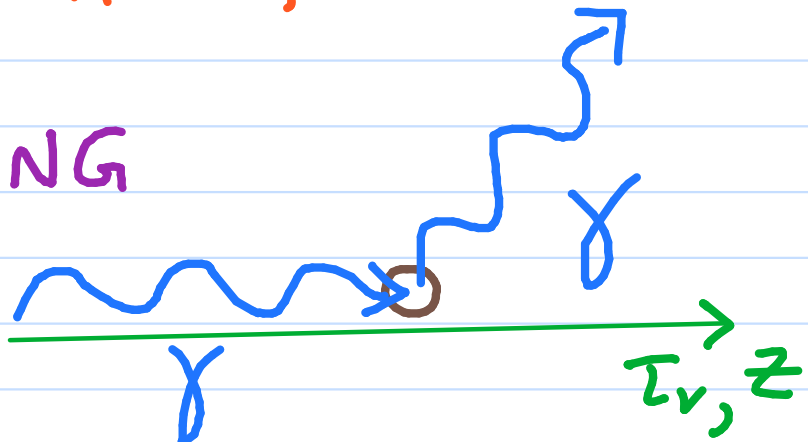
2 TYPES OF EXTINCTION:

1) THERMAL DESTRUCTION



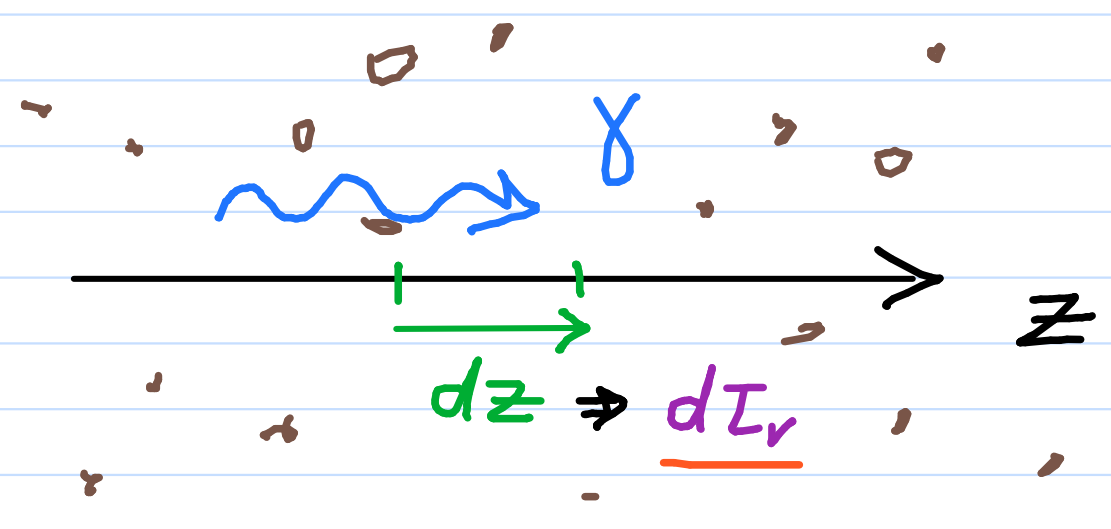
-eg. PHOTO-EXCITATION, -IONIZATION

2) SCATTERING



-eg. THOMSON-, RAYLEIGH- SCATTERING

# MONOCHROMATIC OPTICAL DEPTH ALONG A $\gamma$ PATH, $T_\nu(\nu)$

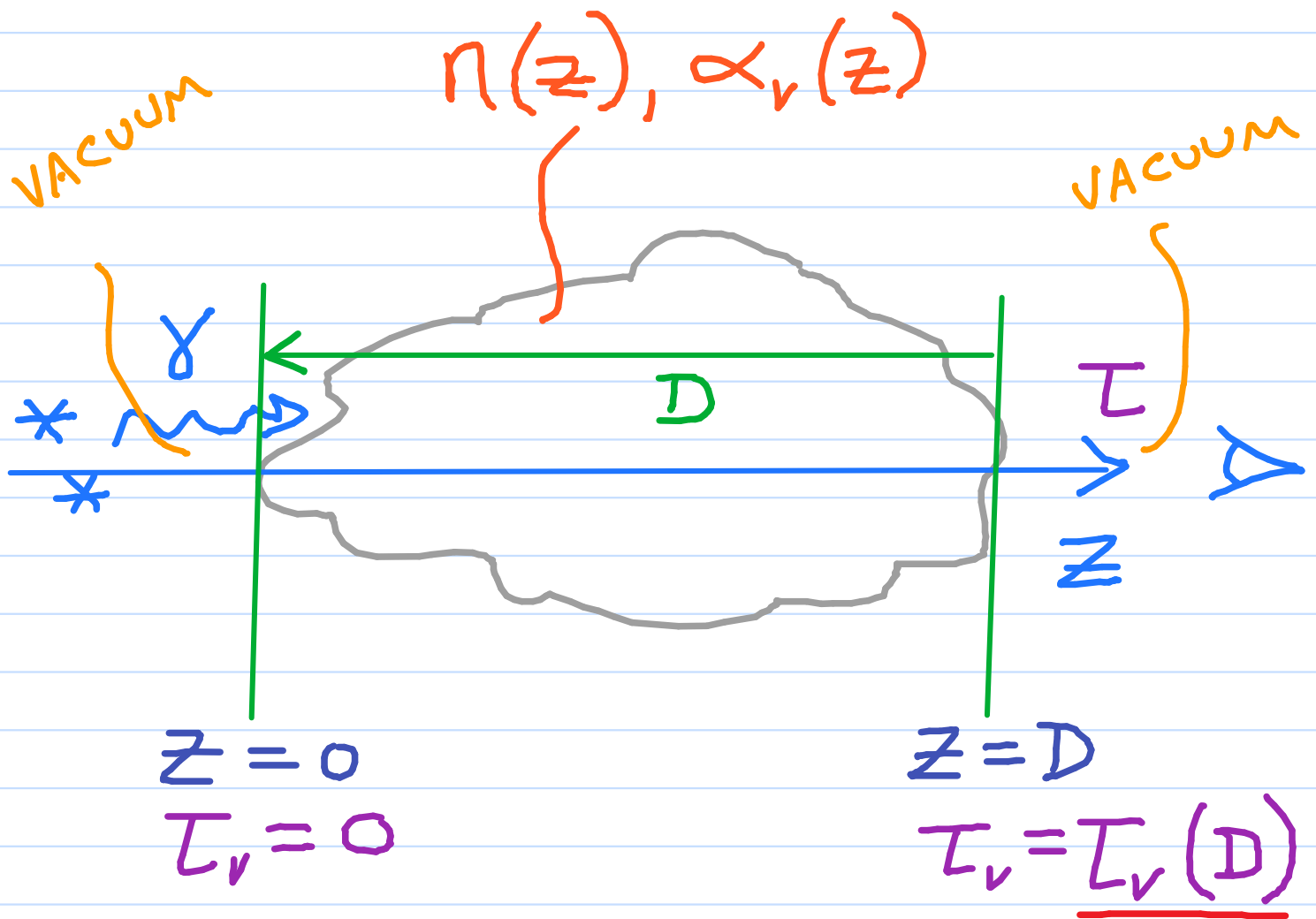


$$dT_\nu(\underline{z}) \equiv \alpha_\nu(\underline{z}) dz$$

$$= \kappa_\nu(\underline{z}) \rho(\underline{z}) dz$$

(UNIT LESS)

MONOCHROMATIC OPTICAL  
THICKNESS,  $T_v(z=D)$ :



$$T_v(D) = \int_{z=0}^D \alpha_v(z) dz = \int_0^D K_v(z) \rho(z) dz$$

$T_v(D) < 1$ : OPTICALLY THIN

⇒ TRANSPARENT

$T_v(D) \gg 1$ : OPTICALLY THICK

⇒ OPAQUE

MEAN OPACITIES:

$$\underline{\underline{\bar{\alpha}}} = \frac{\int_{\nu=0}^{\infty} \overset{\text{WEIGHT } F_n}{W(\nu)} \alpha_{\nu}(\nu) d\nu}{\int_{\nu=0}^{\infty} W(\nu) d\nu} \quad (\text{cm}^{-1})$$

$$\bar{K} = \frac{\bar{\alpha}}{\rho} \quad (\text{cm}^2/\text{g})$$

"GRAY" OPACITY:  $\alpha_{\nu}(\nu) = \bar{\alpha}$

GRAY  $\tau$ -SCALE:

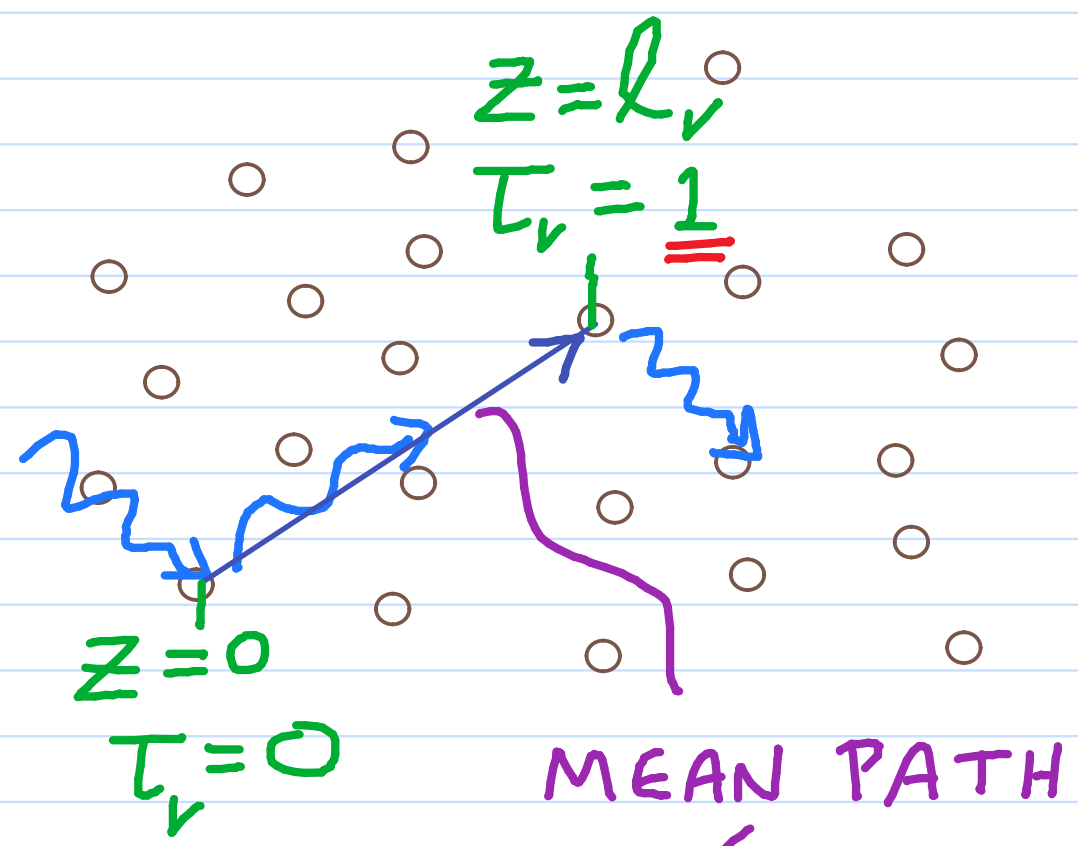
$$d\tau = \bar{\alpha}(z) dz = \bar{K}(z) \rho(z) dz$$

$$\Rightarrow \tau(z) = \int_0^z \bar{\alpha}(z) dz$$

-eg. ROSSELAND OPTICAL DEPTH,  $\tau_{ROS}$

# MONOCHROMATIC MEAN-FREE-PATH,

$l_v$  (cm) :



$$T_v \equiv \int_{z=0}^{\underline{\underline{l_v}}} \alpha_v(z) dz = \underline{\underline{1}}$$

