

EMISSIVITY & EXTINCTION  
COEFFICIENTS:  $\alpha_\nu$  &  $j_\nu$ :

i) b-b TRANSITIONS ( $l \rightleftharpoons u$ )

MONOCHROMATIC VOLUME

EXTINCTION COEFFICIENT,  $\alpha_\nu^l$  ( $\text{cm}^{-1}$ )

$$\alpha_\nu^l(\nu - \nu_0) = \frac{h\nu}{4\pi} \left\{ \underbrace{n_l}_{l} \underbrace{B_{lu}}_{lu} \underbrace{\phi_\nu}_{\nu}(\nu - \nu_0) - \underbrace{n_u}_{u} \underbrace{B_{ul}}_{ul} \underbrace{\chi_\nu}_{\nu}(\nu - \nu_0) \right\}$$

2<sup>nd</sup> TERM: "CORRECTION" FOR STIM.  
EMISSION

- STIM. EM. IS EXACTLY -ve  
EXTINCTION

$$\therefore \alpha_{\nu}^{\downarrow} = \frac{h\nu}{4\pi} n_l B_{lu} \phi_{\nu} \left\{ 1 - \frac{n_u B_{ul} \chi_{\nu}}{n_l B_{lu} \phi_{\nu}} \right\}$$

$$- \frac{B_{ul}}{B_{lu}} = \frac{g_l}{g_u}$$

$$- \text{CRD: } \chi_{\nu} = \phi_{\nu}$$

$$\therefore \alpha_{\nu}^{\downarrow} = \frac{h\nu}{4\pi} n_l B_{lu} \phi_{\nu} \left\{ 1 - \frac{n_u g_l}{n_l g_u} \right\}$$

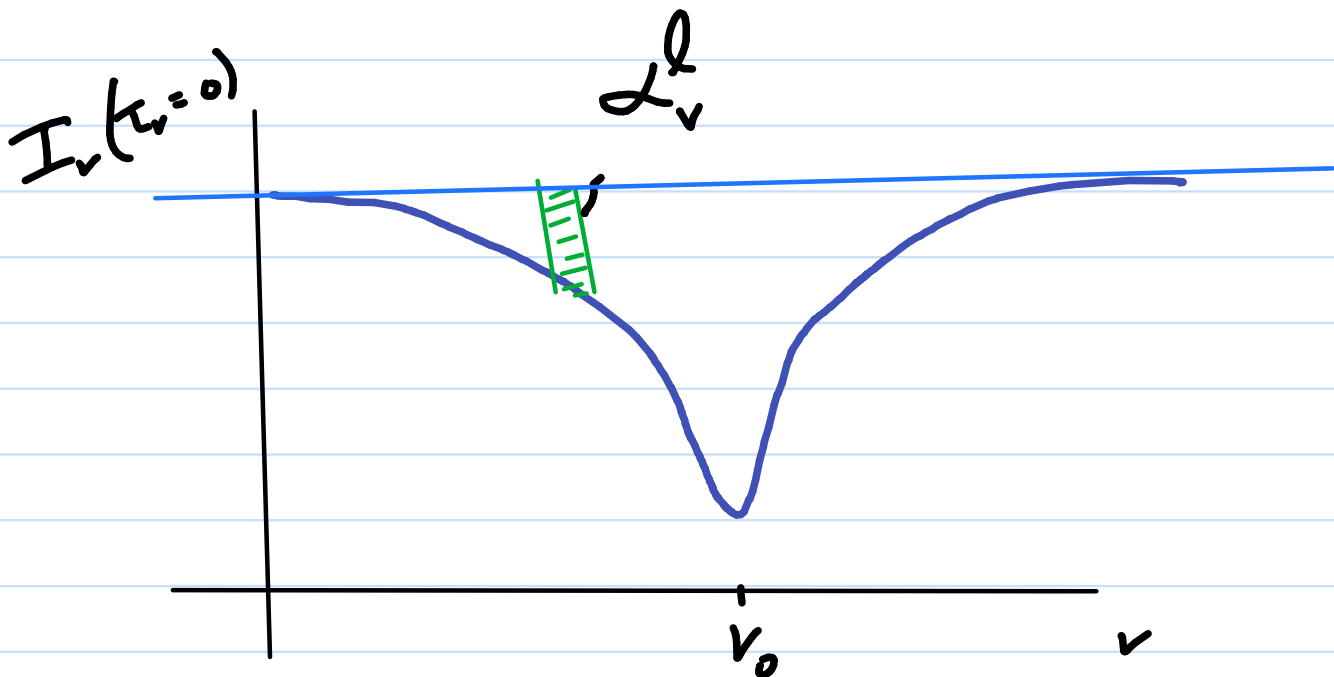
LTE BOLTZMANN DIST:

$$\frac{n_u g_l}{n_l g_u} = e^{-\frac{\overline{\epsilon}_u - \overline{\epsilon}_l}{k T_{\text{KIN}}}}$$

$$\therefore \alpha_{\nu}^l = \frac{h\nu}{4\pi} n_l B_{lu} \phi_{\nu} \left( 1 - e^{-h\nu_0/kT_{kin}} \right)$$

LTE CORRECTION FOR STIM. EM.

$$= \left( 1 - e^{-h\nu_0/kT_{kin}} \right)$$



TOTAL LINE EXTINCTIONCOEFFICIENT,  $\alpha_{\nu_0}^l$  :- ASSUMING CRD:  $\chi_\nu = \phi_\nu$ 

$$\alpha_{\nu_0}^l =$$

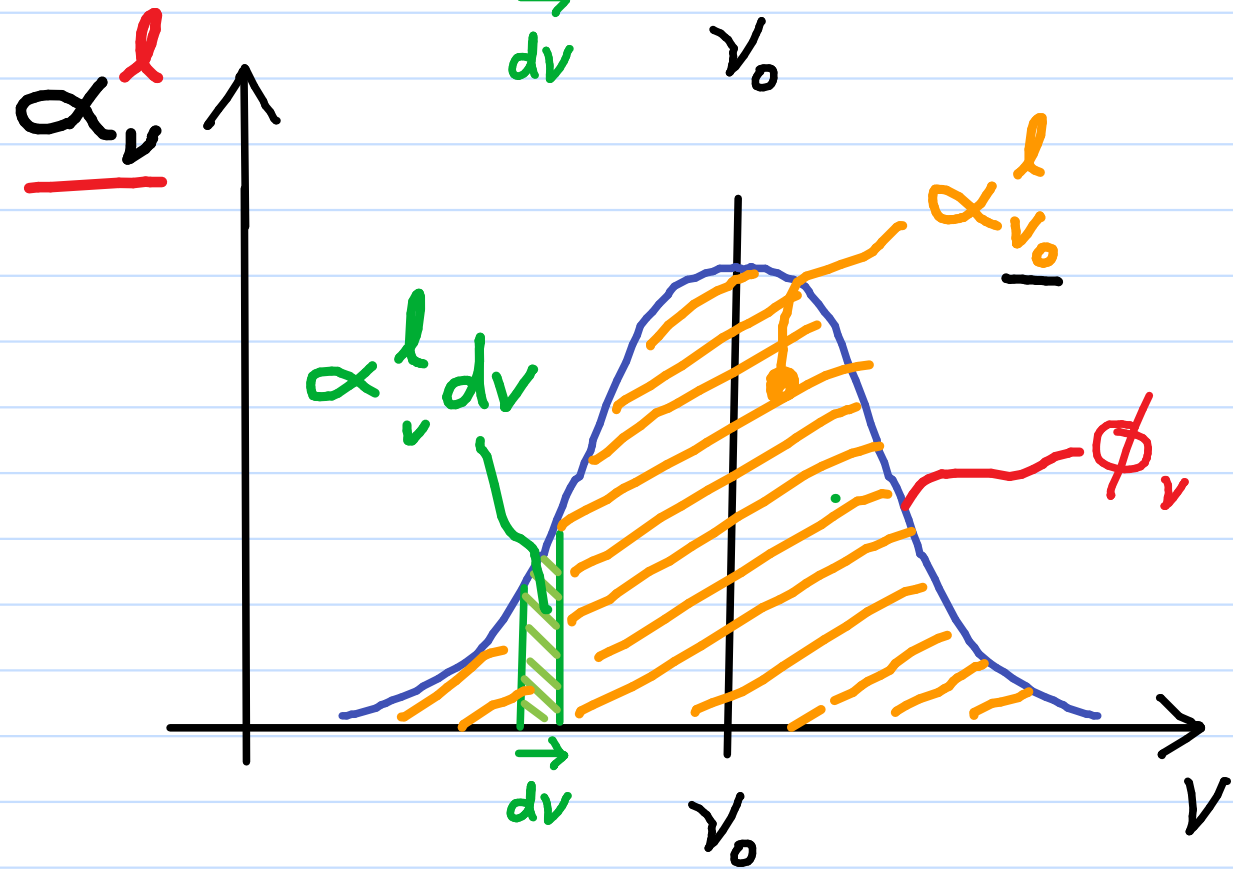
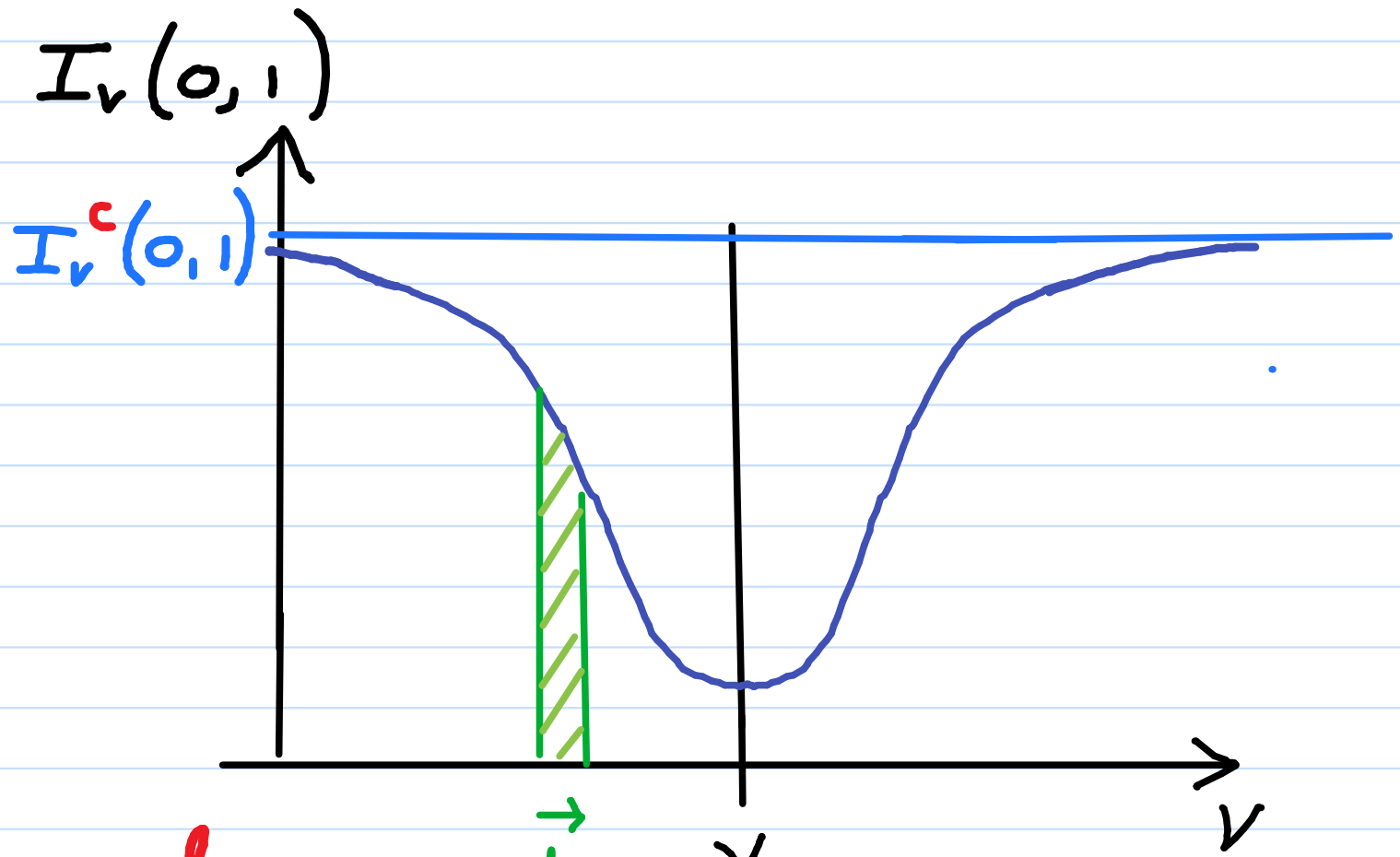
$$\frac{1}{4\pi} (\eta_l B_{lu} - \eta_u B_{ul}) \int_{\nu=0}^{\infty} h\nu \phi_\nu(\nu - \nu_0) d\nu$$

IF LINE NARROW & SYMMETRIC:

$$\alpha_{\nu_0}^l \approx \frac{h\nu_0}{4\pi} (\eta_l B_{lu} - \eta_u B_{ul})$$

- TOTAL TRANSITION "STRENGTH"

# LINE EXTINCTION, $\alpha_\nu^l$ :





# MONOCHROMATIC LINE EXTINCTION

PER PARTICLE,  $\sigma_{\nu}^l$  :

$$\sigma_{\nu}^l(\nu - \nu_0) = \frac{h\nu}{4\pi} B_{lu} \phi_{\nu}(\nu - \nu_0)$$

TOTAL LINE EXTINCTION

CROSS-SECTION,  $\sigma_{\nu_0}^l$  ( $\text{cm}^2$ )

$$\sigma_{\nu_0} = \frac{B_{lu}}{4\pi} \int_0^{\infty} h\nu \phi_{\nu}(\nu - \nu_0) d\nu$$

$$\approx \frac{h\nu_0}{4\pi} B_{lu}$$

# OSCILLATOR STRENGTH, $f_{lu}$ (UNITLESS)

$$\frac{\pi e^2}{m_e c} \underline{f_{lu}} \equiv \frac{h\nu_0}{4\pi} B_{lu} \approx \sigma_{\nu_0}^l$$

RECALL:  $A_{ul} = B_{lu} \frac{g_l}{g_u} \frac{2h\nu_0^3}{c^2}$

$$\therefore A_{ul} = \frac{(g_l f_{lu})}{g_u} (h\nu_0)^2$$

"gf-VALUE"  $\equiv g_l \underline{f_{lu}}$

MONOCHROMATIC VOLUME

EMISSION COEFFICIENT,  $j_{\nu}^l$   
 (erg/s/cm<sup>3</sup>/STER/Hz)

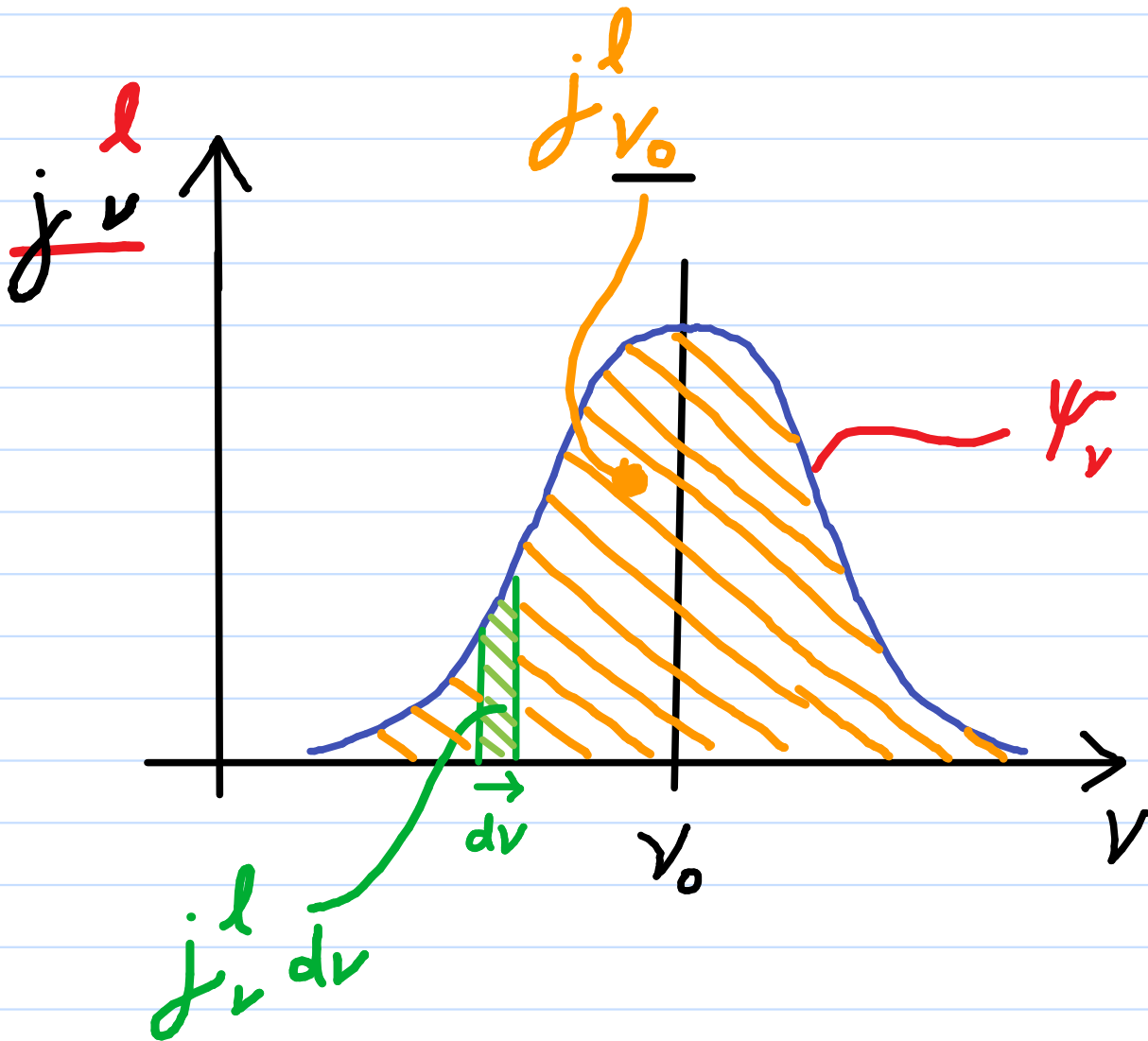
$$j_{\nu}^l(\nu - \nu_0) = \frac{h\nu}{4\pi} (n_u A_{ul} \Psi_{\nu}(\nu - \nu_0))$$

TOTAL LINE EMISSIVITY,  $j_{\nu_0}^l$ :

$$j_{\nu_0}^l = \frac{n_u A_{ul}}{4\pi} \int_0^{\infty} h\nu \Psi_{\nu}(\nu - \nu_0) d\nu$$

$$\approx \frac{h\nu_0}{4\pi} n_u A_{ul}$$

# LINE EMISSIVITY:



# MONOCHROMATIC LINE SOURCE $f_n, S_r^l$

$$S_r^l(\nu - \nu_0) \equiv \frac{j r_l^l(\nu - \nu_0)}{\alpha_r^l(\nu - \nu_0)}$$

$$= \frac{(\cancel{h\nu/4\pi}) n_u A_{ul} \psi_r}{(\cancel{h\nu/4\pi}) \{n_l B_{lu} \phi_r - n_u B_{ul} \chi_r\}}$$

- ASSUME CRD:  $\psi_r = \chi_r = \underline{\phi_r}$

$$\therefore S_{\nu_0}^l = \frac{n_u A_{ul}}{n_l B_{lu} - n_u B_{ul}}$$

$$= \frac{A_{ul}/B_{ul}}{n_l B_{lu}/n_u B_{ul} - 1}$$

RECALL:

$$\frac{A_{ul}}{B_{ul}} = \frac{2h\nu_0^3}{c^2} ; \quad \frac{B_{lu}}{B_{ul}} = \frac{g_u}{g_l}$$

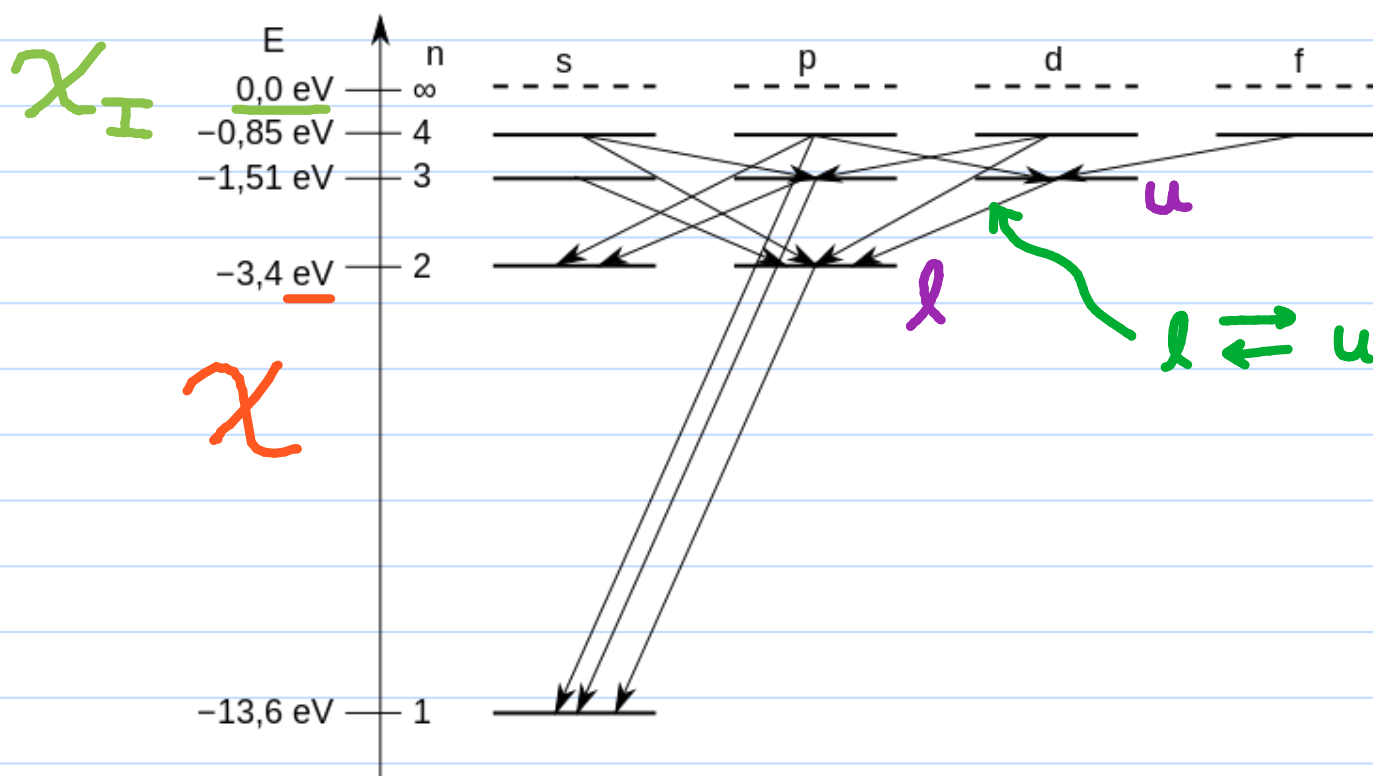
$$\therefore S_{\nu_0}^l = \frac{2h\nu_0^3}{c^2} \frac{1}{\frac{g_u n_l}{g_l n_u} - 1}$$

IN LTE:  $\frac{g_u n_l}{g_l n_u} = e^{h\nu_0/kT_{\text{KIN}}}$

$$\therefore S_{\nu_0}^l = \frac{2h\nu_0^3}{c^2} \frac{1}{e^{h\nu_0/kT} - 1} = B_{\nu_0}(T_{\text{KIN}})$$

Eg. H I:

## ATOMIC E-LEVELS & b-b TRANSITIONS



CREDIT: WIKIMEDIA COMMONS